

Mixer Sizing Methods

Four different sizing criteria

- *Velocity*
- *Shear Stress*
- *Yield Stress*
- *Mixing Time*

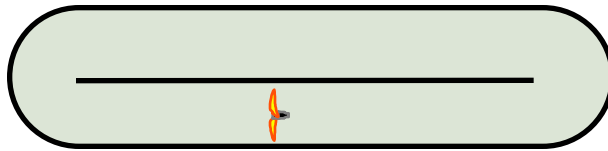
Velocity

Mixing Duties

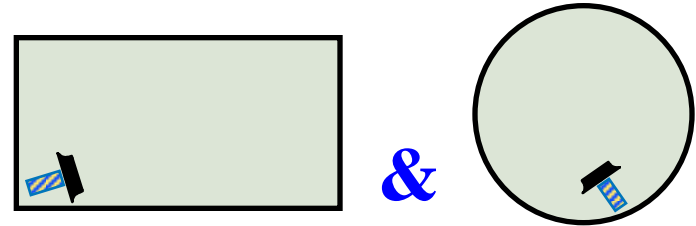
- Circulation
 - u specified
 - heat or mass transfer specified
 - ...
- Homogeneous suspension
 - u depends on u_{settl} and tank geometry
 - Standard u values in biological treatment systems

Velocity

Required thrust = (Size of Mixer) = $F_{\text{req}} \sim u^2 k$



- **Losses (k) - Racetrack**
 - Bends
 - Friction wall & bottom
 - Aeration
 - Obstacles



- **Losses (k) - Other tanks**
 - Tank factor (geometry)
 - Propeller factor
 - Aeration
 - Obstacles

Shear Stress

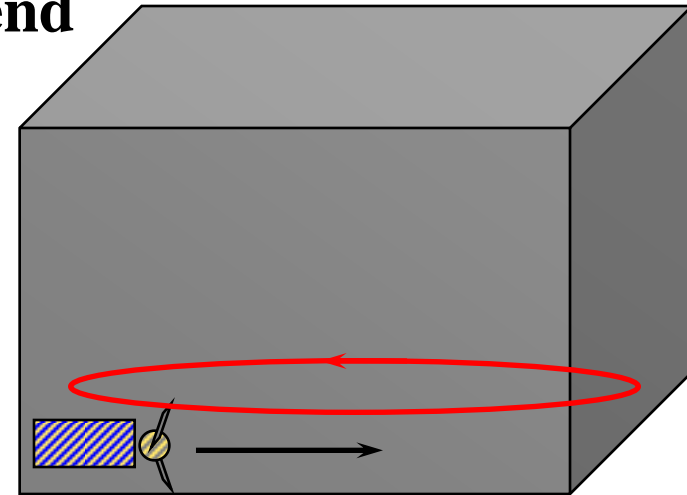
Mixing Duties

- Off bottom suspension & Resuspension of sediment
 - Shear Stress calculated
 - Shear Stress measured
 - By experience
- Erosion and transport of sediments

Shear Stress

Required thrust = (Size of Mixer) = $F \sim \tau_s$

- τ_s = Requires Shear stress to resuspend
 - measured
 - calculated
 - Experience



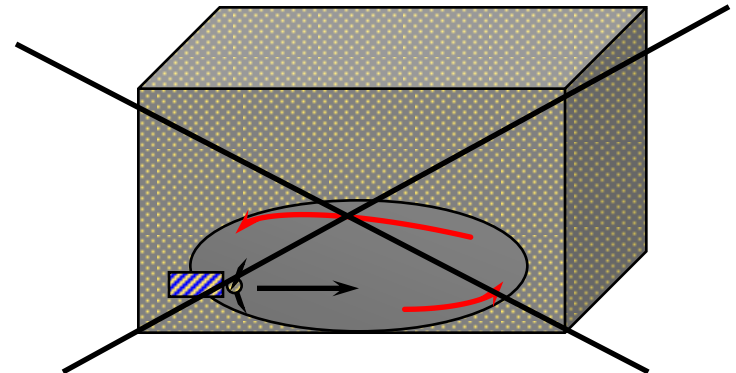
Flygt

Yield Stress

For mixing to be possible, the fluid must move at all. If it has a finite **Yield Stress**, this must be overcome. Hence this is an additional mixing criterion, often decisive.

Applications

- Thickened sludge
- Paper pulp
- Drilling mud
- Slurries ...



Yield Stress

Required thrust = (Size of Mixer) = $F \sim \tau_y$

- where τ_y is
 - Calculated or measured for municipal sludge, drilling mud & paper pulp
 - Specified by client
 - Measured by e.g. ITT Flygt Application Lab / known otherwise

Mixing Time

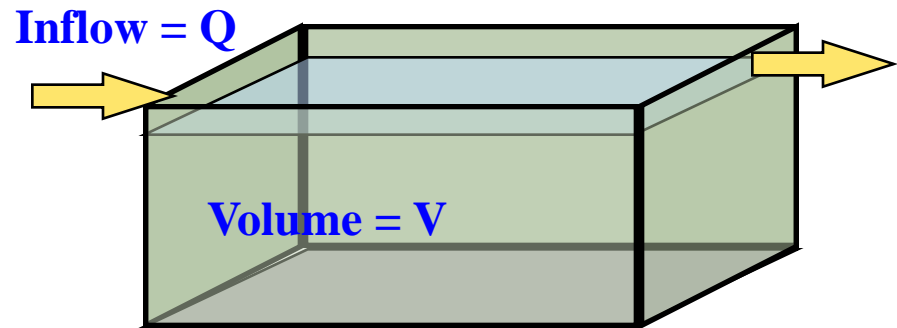
Mixing Duties

- Required blending time Θ specified or given by
 - **Throughflow**; fluid leaving tank is mixed to a certain homogeneity ξ_b .
 - **Batch**; customer requires a certain maximum time Θ and a certain minimum homogeneity ξ_b .

Mixing Time

Required thrust = (Size of Mixer) = $F \sim 1 / \Theta^2$

- Θ^2 Specified mixing time
 - Given by customer
 - Given by process
 - Retention time



Retention time = V/Q

Quantified mixing demands

- **Velocity** $F \sim u^2$
- **Shear stress** $F \sim \tau_s$
- **Yield stress** $F \sim \tau_y$
- **Time** $F \sim 1 / \Theta^2$

Extra study

Channels - Required thrust

“The velocity Solver”

The required thrust is

$$F_{req} = \frac{\rho U^2}{2} A_b k$$

ρ is the liquid density (1000 kg/m³ for water)

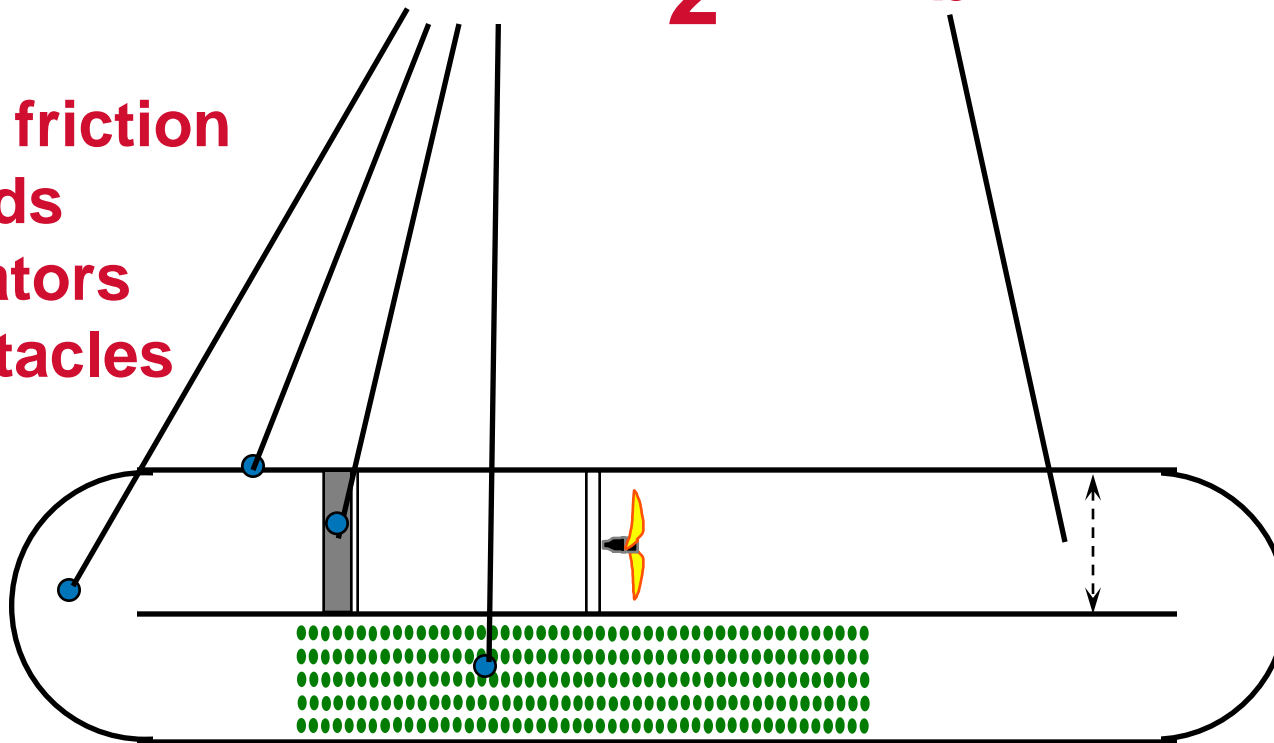
$k = k_f + k_b + k_{aer} + k_o$ are loss factors due to friction, bends, aerators, other obstacles.

A_b is the bulk flow area (projected area of cross section of main flow)

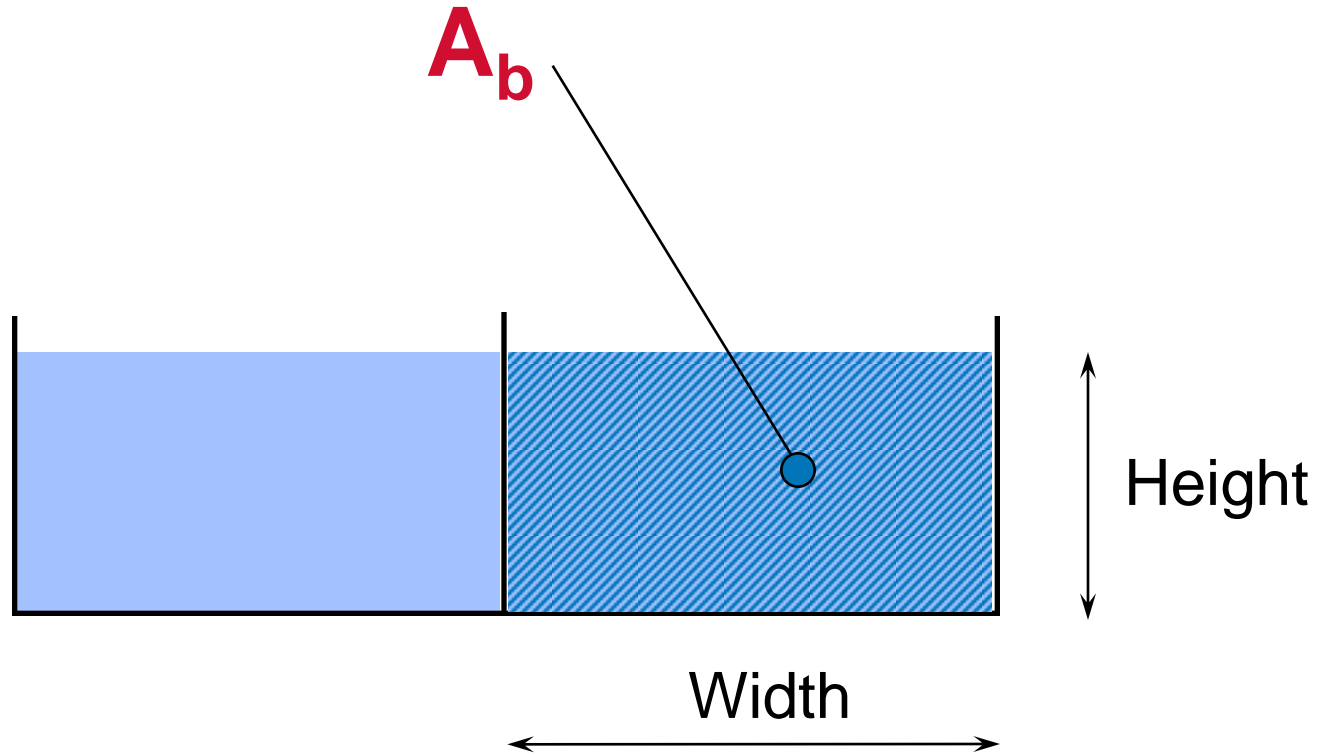
A racetrack example

$$F = k \cdot \frac{\rho u^2}{2} \cdot A_b$$

- Wall friction
- Bends
- Aerators
- Obstacles



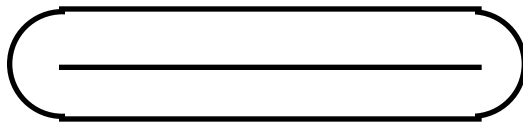
Bulk flow area



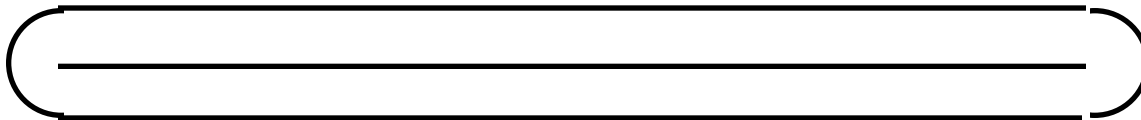
Wall friction



Surface roughness



Length of flow loop



Friction loss factor

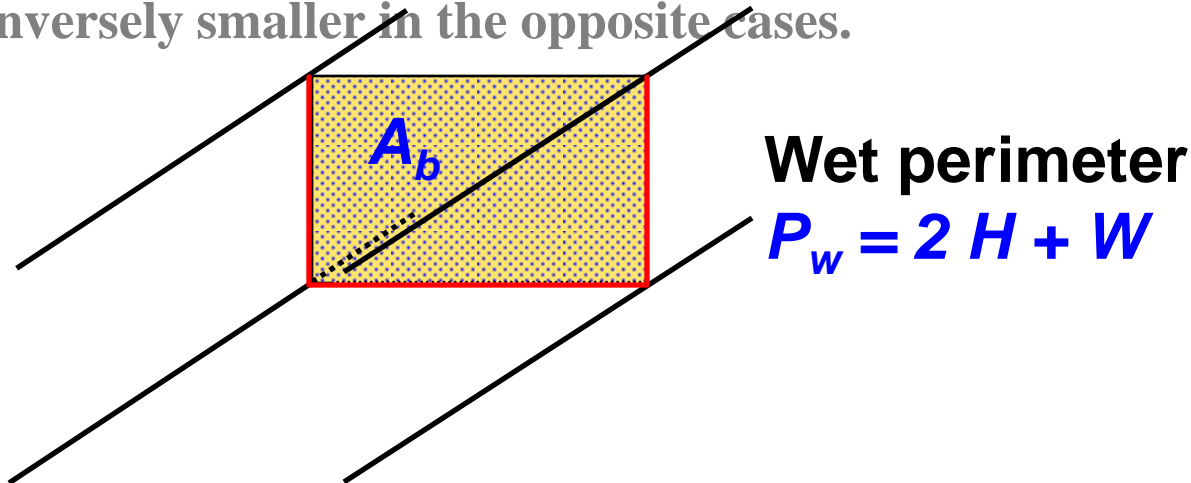
$$k_f = L_{tot} / (M R_h)$$

L_{tot} total mean length of channel

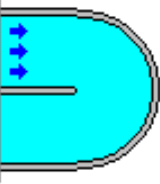
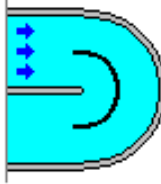
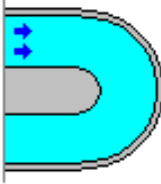
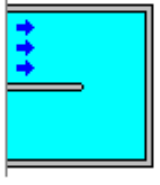
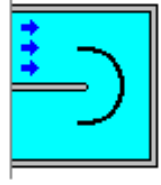
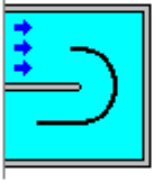

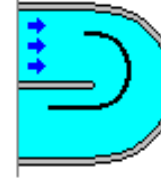
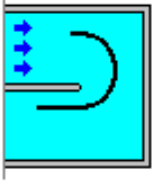
$R_h = A_b / P_w$ hydraulic radius

$M \approx 80$ (Inverse) Manning number

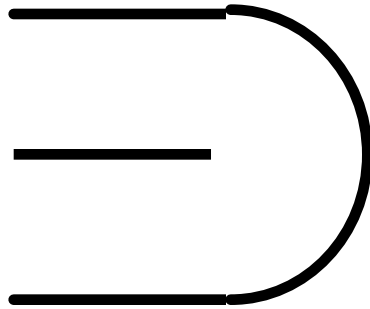
M is larger for very small channels or very smooth surfaces, and conversely smaller in the opposite cases.



Bend loss factors k_b

 <p>1.5</p>	 <p>0.6</p>	 <p>0.3 -- 1.5</p>
 <p>2.5</p>	 <p>1.0</p>	 <p>0.8</p>
 <p>0.5</p>	 <p>1.1</p>	 <p>1.4</p>

Bend losses



$$k_b = 1,5$$

Aerator losses

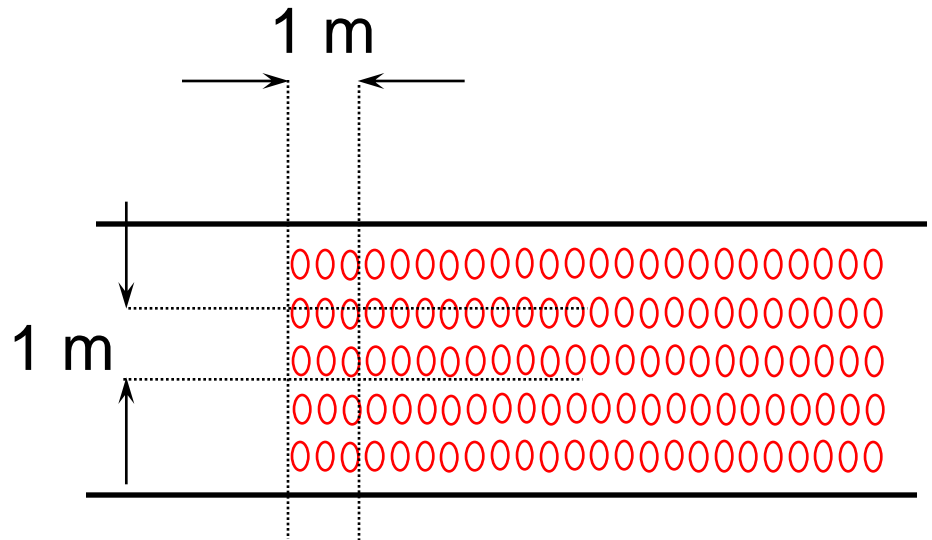
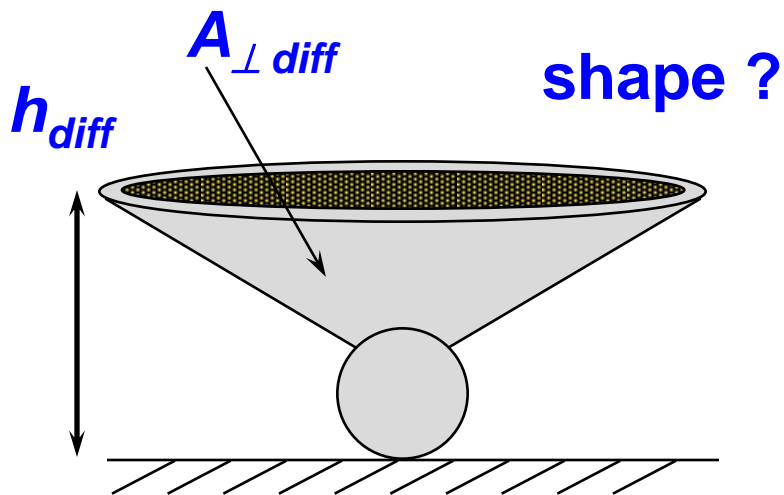
- **Diffusers act as flow obstacles**
- **Bubble columns increase the hydraulic losses by**
 - causing counterflow to the bulk flow
 - causing velocity distributions that increase losses on the bottom and on the diffusers



Aeration loss factor k_{aer}

Bottom diffuser geometry

Bottom diffuser density in grid (m^{-2})



Aeration loss factor k_{aer}

- # grids
- Bottom coverage (%)
- Air flow Q_{air} (Nm^3/h)
- Bulk flow velocity u

→ k_{aer}

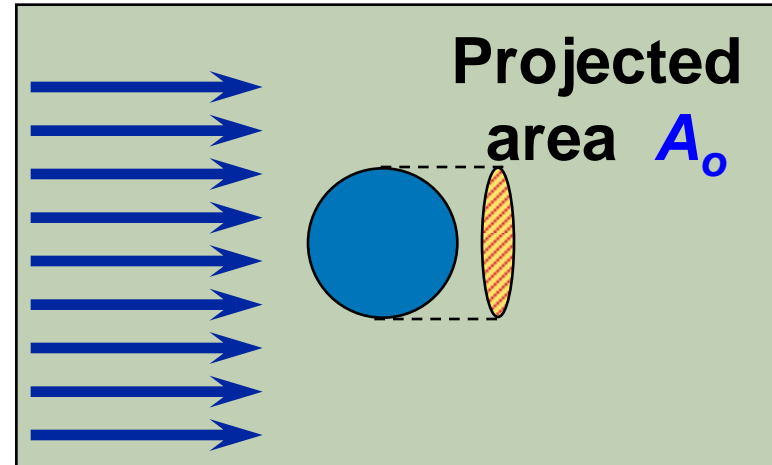
Obstacle loss factor k_o

The loss force from an obstacle is

$$F_o = \frac{\rho u^2}{2} A_o c_D,$$

And, to use A_b in the F_{req} - formula,

$$k_o = c_D A_o / A_b.$$



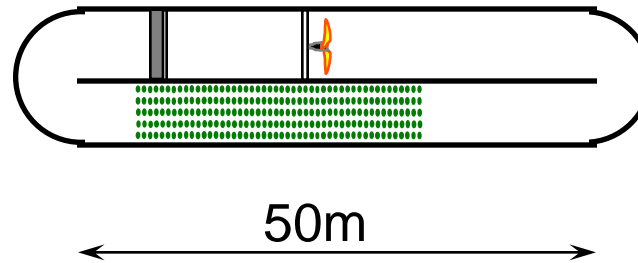
c_D is typically between 1.0 and 2.0.

For the pipe, say $A_o = 6.0 \times 0.5 \text{ m}^2$, $c_D = 1.0$

$$k_o = c_D A_o / A_b = 0.125$$

A racetrack example

1 grid Sanitaire diff,
20% covered area

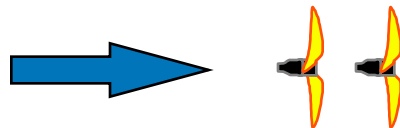


6m
6m
H=4m

$$F = k \cdot \frac{\rho u^2}{2} \cdot A_{bulk}$$

$$F = (0.87 + 2 \cdot 1.5 + 0.55 + 0.125) \cdot 1000 \cdot \frac{0.30^2}{2} \cdot (6 \cdot 4) = 4774 \text{ N}$$

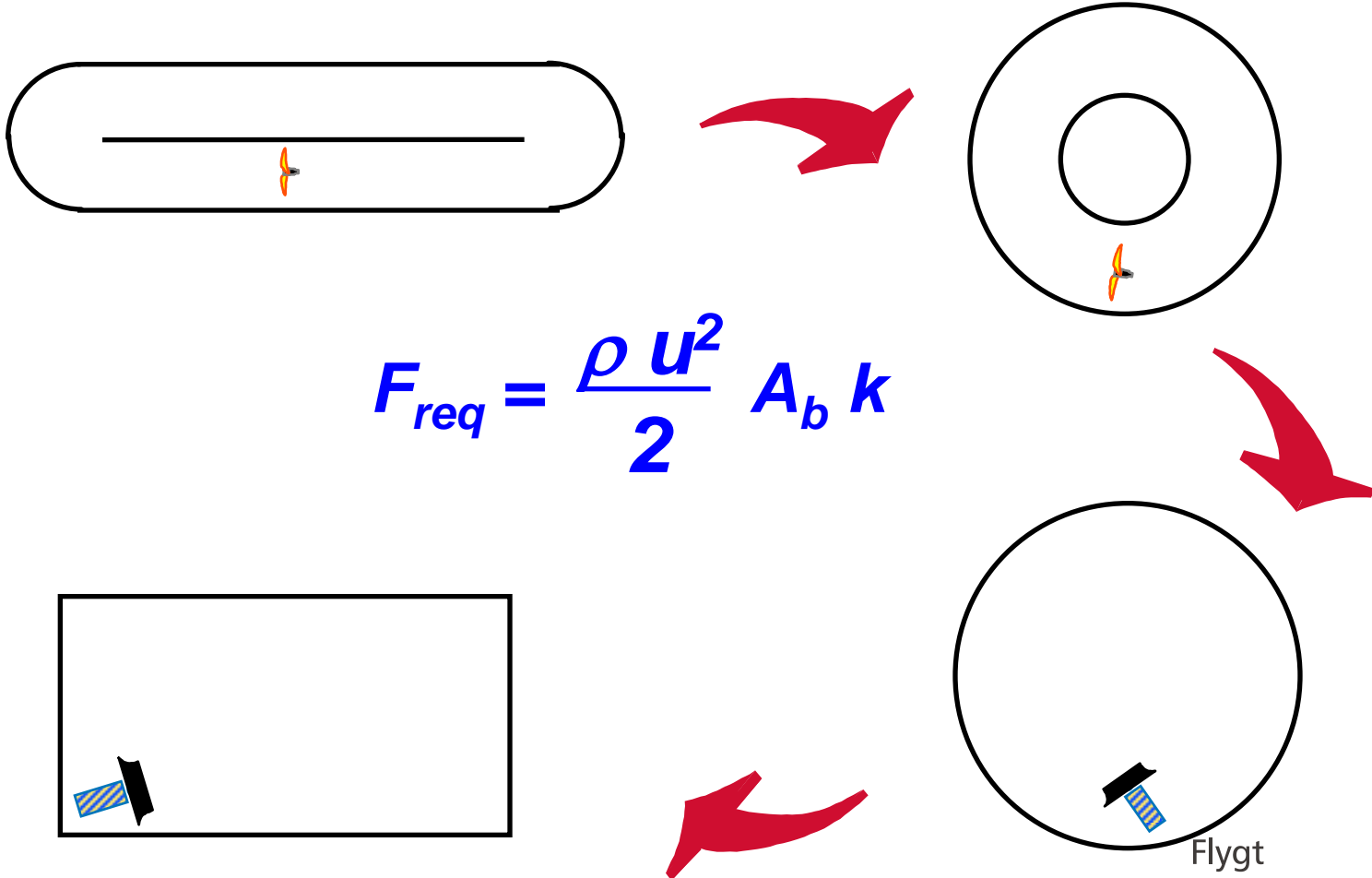
friction bends aerators obstacle



2 units 4430

Other tank shapes

The same principles as in channels....



$$F_{req} = \frac{\rho u^2}{2} A_b k$$

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